

ROTHAMSTED EXPERIMENTAL STATION
(LAWES AGRICULTURAL TRUST)

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Professor R.A. Fisher,
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Gower Street,
London, W.C.1.

HARPENDEN
HERTS

12th February, 1934.

Dear Fisher,

Thanks very much for letting me see the M.S. of the χ^2 correction paragraph, which I return herewith. I haven't had any time to search for examples, and no suitable one has come my way. You doubtless got my letter re Mainland as a possible fund of examples. I think it might be worth while including an example of his if by any chance he turns up a more suitable one. Your present example ^(as you point out) has the disadvantage of giving a probability in the region where disagreement with the corrected χ^2 does not matter, and where ~~it does~~ not claim that even the corrected value gives a tolerable approximation.

As regards limits I have tentatively come to the conclusion that "expected" values are a good criterion and that with no expected value less than unity the correction gives an adequate approximation. It also appears that ^{(with expected values of}

5 or even considerably higher the uncorrected value is very misleading. The values for the symmetrical cases,

| | | |
|--------|----|-----|
| χ | | 50 |
| | | 50 |
| <hr/> | | |
| 50 | 50 | 100 |
| (1) | | |

| | | |
|--------|----|----|
| χ | | 10 |
| | | 10 |
| <hr/> | | |
| 10 | 10 | 20 |
| (2) | | |

for example, are shown in the accompanying table. It might be worth giving a word of warning on this point.

I am sorry I have not yet applied the finishing touches. Routine work at the moment is intollerably pressing, but I have written up most of it now, and have only to make certain that unity is a good limiting value.

Yours sincerely,



P.S. I enclose a table belonging to the paper on 6 x 6 Latin squares which you left here.

Table

(1)

| χ^2 | True P | $P(\chi^2)$ | Corrected $P(\chi^2)$ |
|----------|--------|-------------|--------------------------|
| 16, 34 | .0006 | .0003 | .0007 |
| 17, 33 | .0026 | .0014 | .0027 |
| 18, 32 | .0090 | .0051 | .0093 |
| 19, 31 | .0274 | .0164 | .0278 |
| 20, 30 | .0714 | .0455 | .0718 |
| 21, 29 | .1612 | .1096 | .1615 |
| 22, 28 | .3174 | | .3173 |
| 23, 27 | .5488 | | .5485 |
| 24, 26 | .8416 | | .8415 |
| 25 | 1.0000 | | 1.0000 |

(2)

| χ^2 | True P | $P(\chi^2)$ | Corrected $P(\chi^2)$ |
|----------|--------|-------------|--------------------------|
| 4, 16 | .0004 | .00015 | .0006 |
| 5, 15 | .0038 | .0016 | .0044 |
| 6, 14 | .0256 | .011 | .0268 |
| 7, 13 | .1128 | .057 | .1139 |
| 8, 12 | .3430 | .206 | .3428 |
| 9, 11 | .7524 | | .7519 |
| 10 | 1.0000 | | 1.0000 |