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1  
2 **BEHAVIOR OF FRP-CONFINED NORMAL- AND HIGH-STRENGTH CONCRETE**  
3 **UNDER CYCLIC AXIAL COMPRESSION**

4  
5 Togay Ozbakkaloglu<sup>1</sup> and Emre Akin<sup>2</sup>

6  
7 **ABSTRACT**

8 An important application of fiber reinforced polymer (FRP) composites is as a confining material  
9 for concrete, in both the seismic retrofit of existing reinforced concrete columns and in the  
10 construction of concrete-filled FRP tubes as earthquake-resistant columns in new construction. The  
11 reliable design of these structural members against earthquake-induced forces necessitates a clear  
12 understanding of the stress-strain behavior of FRP-confined concrete under load cycles. This paper  
13 presents the results of an experimental study on the behavior of FRP-confined normal- and high-  
14 strength concrete under axial compression. A total of 24 aramid and carbon FRP-confined concrete  
15 cylinders with different concrete strengths and FRP jacket thicknesses were tested under monotonic  
16 and cyclic loading. Examination of the test results have lead to a number of significant conclusions  
17 in regards to both the trend and ultimate condition of the axial stress-strain behavior of FRP-  
18 confined concrete. These results are presented and a discussion is provided on the influence of the  
19 main test parameters in the observed behaviors. The results are also compared with two existing  
20 cyclic axial stress-strain models for FRP-confined concrete.

21  
22 **KEYWORDS:** Fiber reinforced polymers; Concrete; High-strength concrete; Confinement; Cyclic  
23 loading; Stress-strain behavior.

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## 1 INTRODUCTION

2 Owing to their favorable material properties, fiber reinforced polymer (FRP) composites have  
3 become increasingly popular in the construction industry over the last two decades. An important  
4 application of FRP composites is as a confining material for concrete, in both the seismic retrofit of  
5 existing reinforced concrete columns and in the construction of concrete-filled FRP tubes as  
6 earthquake-resistant columns in new construction. For the safe and reliable design of these  
7 structural members, it is necessary to properly understand and model the stress-strain behavior of  
8 FRP-confined concrete. Of particular importance is the understanding of the behavior of FRP-  
9 confined concrete under cyclic axial compression for the seismic retrofit and design of these  
10 members.

11  
12 The monotonic axial stress-strain behavior of FRP-confined concrete has been studied extensively  
13 over the past two decades, which have lead to the development of over 70 stress-strain models (e.g.,  
14 Samaan et al. 1998; Xiao and Wu 2000; Fam and Rizkalla 2001; Lam and Teng 2003; Binici 2005;  
15 Jiang and Teng 2006; Fahmy and Wu 2010; Xiao et al. 2010). In contrast, only a few studies have  
16 so far investigated the behavior of FRP-confined concrete under cyclic axial compression  
17 (Mirmiran and Shahawy 1997; Rodrigues and Silva 2001; Rousakis 2001; Ilki and Kumbasar 2003;  
18 Shao et al. 2006; Lam et al. 2006; Lam and Teng 2009; Abbasnia and Ziaadiny 2010) and, to the  
19 best knowledge of the authors, only two analytical cyclic stress-strain models (Shao et al. 2006,  
20 Lam and Teng 2009) have been proposed in the open literature. While these studies have provided  
21 valuable insights into certain aspects of the problem, there are a number of other important aspects,  
22 such as the influence of the concrete strength and type of FRP, that are yet to be explored.

23  
24 Not unlike that of FRP, the popularity of high-strength concrete (HSC) in the construction industry  
25 has been on a steady incline during the last two decades. It is now understood that HSC offers  
26 superior performance and economy over normal-strength concrete (NSC) when used in the

1 construction of bridges and multi-story buildings. However, HSC structural members are known to  
2 exhibit brittle behavior, which jeopardizes their use in seismically active regions. Yet, it is well  
3 established that lateral confinement of concrete can greatly enhance its ductility; though, it is also  
4 established that HSC require more confinement than NSC because the confinement demand of  
5 concrete increases proportionally with its strength. Indeed, experimental studies conducted by  
6 Ozbakkaloglu and Saatcioglu (2006, 2007) on the seismic behavior of FRP-confined HSC columns  
7 demonstrated that the lateral deformation capacity of HSC columns can be substantially increased  
8 by the use of FRP tubes as concrete confinement. The majority of the existing studies on the axial  
9 compressive behavior of FRP-confined concrete have focused on NSC with strengths less than 55  
10 MPa, and only a few studies have been concerned with FRP-confined HSC (Berthet et al. 2005;  
11 Mandal et al. 2005; Almusallam 2007; Eid et al 2009; Vincent and Ozbakkaloglu 2009; Wu et al.  
12 2009; Cui and Sheikh 2010; Xiao et al. 2010). As has also been recently reported by Xiao et al.  
13 (2010), existing test results are insufficient for clear understanding of the axial compressive  
14 behavior of FRP-confined HSC. Likewise, a review of the existing literature indicates that the  
15 majority of the existing studies on the axial compressive behavior of FRP-confined concrete have  
16 focused on carbon and glass FRP (CFRP and GFRP) confined concrete, with the behavior of  
17 concretes confined by other composite materials, such as aramid FRP (AFRP) or high-modulus  
18 CFRP (HM CFRP), receiving relatively limited attention.

19

20 This paper presents the results of an experimental study which was aimed at filling the existing  
21 research gaps outlined above. The experimental program focused on the behavior of CFRP-  
22 confined HSC and AFRP-confined NSC and HSC under monotonic and cyclic axial compression,  
23 and it was the first comprehensive study reported in the literature on the axial cyclic behavior of  
24 FRP-confined HSC. The results of the experimental program are first presented, followed by a  
25 discussion on the influence of the main test parameters on the test results. These results are then  
26 compared with two cyclic axial stress-strain models proposed for FRP-confined concrete.

# 1 **EXPERIMENTAL PROGRAM**

## 2 **Test Specimens and Materials**

3 A total of 24 FRP-confined concrete cylinders with a concrete core diameter of 152.5 mm and a  
4 height of 305 mm were manufactured and tested under axial compression. The test parameters  
5 included the concrete compressive strength (i.e., NSC and HSC), type of FRP material (i.e., CFRP  
6 and AFRP), FRP thickness (i.e., 2 to 6 layers), and loading pattern (i.e., axial monotonic and axial  
7 cyclic).

8  
9 The specimens were prepared using NSC and HSC mixes, with average unconfined concrete  
10 compressive strengths 39 MPa and 103 MPa attained during the period of testing. Both mixes  
11 consisted of crushed bluestone as the coarse aggregate with a nominal maximum size of 10 mm.  
12 Silica fume was added to the HSC mix at 8 percent of the binder content by weight. The NSC  
13 specimens were cast of a single batch, whereas two separate batches were prepared for the HSC  
14 specimens. The testing of the HSC specimens started right after the attainment of the 28-day  
15 strength and continued for approximately 3 weeks. Concrete cylinder tests have been conducted  
16 through the testing program to accurately record the variations in the strength of unconfined  
17 concrete during testing. The unconfined concrete strengths  $f'_{co}$  at the day of testing are reported  
18 together with the corresponding axial strains  $\varepsilon_{co}$  in Table 1 for each specimen.  $\varepsilon_{co}$  values were not  
19 measured directly for all the control specimens but were calculated using the expression given by  
20 Tasdemir (1998).

21

22 The specimens were confined by either CFRP or AFRP jackets. AFRP was used for the  
23 confinement of both NSC and HSC, whereas CFRP was used only for the jacketing of HSC  
24 specimens. In determining the number of FRP layers of the specimens, due consideration was given  
25 to the well-understood influence of the concrete strength on the confinement demand (Martinez et  
26 al. 1984; Yong et al. 1988; Razvi and Saatcioglu 1994). The FRP jackets of the 22 of the specimens

1 were formed by manually wrapping impregnated FRP sheets around the concrete cylinders in the  
2 hoop direction. Two of the specimens (i.e., H-C-4L-M1 and H-C-6L-M2) were confined by  
3 formerly manufactured CFRP tubes instead of wrapping. Similar to the wrapped specimens, these  
4 tubes were prepared using a manual wet lay-up process by wrapping epoxy resin impregnated fiber  
5 sheets around precision-cut high-density Styrofoam templates in the hoop direction. An overlap  
6 length of 100 mm was provided in all specimens to prevent premature debonding failure.  
7 Specimens confined with 2 and 3 layers of FRP were wrapped with a single FRP sheet  
8 continuously, whereas specimens confined with 4 and 6 layers of FRP were wrapped by two FRP  
9 sheets, and hence had two overlap regions. The details of the test specimens are given in Table 1  
10 and the properties of the unidirectional carbon and aramid fiber sheets used in the manufacturing of  
11 the FRP jackets are provided in Table 2. Two nominally identical specimens were tested for each  
12 unique specimen/loading configuration.

13

#### 14 **Specimen Designation**

15 The specimens in Tables 1 and 3 were labeled as follows: letters N and H were used to label "NSC"  
16 and "HSC". This was followed by a letter "A" or "C", which were used in labeling "aramid" and  
17 "carbon" FRP. The number of FRP layers was given next, and was followed by a letter M for  
18 "monotonic" or C for "cyclic" loading. The final numbers 1 or 2 were used to make distinction  
19 between two nominally identical specimens. For instance, N-A-2L-C1 is the first of the two  
20 identical specimens that were made of NSC confined with 2-layers of AFRP, and tested under  
21 cyclic loading.

#### 22 **Test Setup and Instrumentation**

23 Axial deformations of the specimens were measured with four linear variable displacement  
24 transducers (LVDTs), which were mounted at the corners between the loading and supporting steel  
25 plates of the test machine as shown in Fig. 1. The recorded deformations were used in the  
26 calculation of the average axial strains along the height of the specimens. In addition, the specimens

1 were also instrumented at the mid-height with two unidirectional strain gauges with a gauge length  
2 of 20 mm to measure axial strains. These strain gauge readings were used to correct the LVDT  
3 measurements at the early stages of loading, where additional displacements due to closure of the  
4 gaps in the setup were also recorded by the LVDTs. Transverse strains were measured by three  
5 unidirectional strain gauges having a gauge length of 20 mm that were bonded on the FRP jacket  
6 outside the overlap region.

7  
8 The specimens were tested under axial compression using a 5000 kN capacity universal testing  
9 machine. Initial elastic portion of monotonic and cyclic loading and unloading/reloading cycles of the  
10 cyclic loading were performed with load control at 3 kN per second, whereas displacement control  
11 was used at approximately 0.01 mm per second for the entire response of monotonically loaded  
12 specimens beyond initial softening, and for the segments between each unloading curve for cyclically  
13 loaded specimens. Prior to testing, all specimens were capped at both ends with a thin layer of high-  
14 strength capping material to ensure uniform distribution of the applied pressure, and the load was  
15 applied directly to the concrete core thorough the use of two precision-cut high-strength steel discs  
16 with 150 mm diameter and 15 mm thickness, as illustrated in Fig.1. For 12 of the specimens,  
17 loading was increased monotonically until failure. For the remaining twelve specimens, cyclic  
18 compression involving unloading and reloading cycles was applied at approximately 0.15% axial  
19 strain intervals. These specimens were subjected to a single unloading/reloading cycle at each  
20 prescribed axial strain level. A small axial load of 30 kN was maintained during the  
21 unloading/reloading cycles to prevent any undesired movement in the specimen. Test setup and  
22 instrumentation are shown in Fig. 1.

23

## 24 **TEST RESULTS**

### 25 **Failure mode**

1 Typical failures of the test specimens are shown in Fig. 2. All of the specimens failed by rupture of  
2 the FRP jacket. As can be seen in Fig. 2, two different types of damage were observed in the  
3 concrete depending on its compressive strength. Concrete shear cones were formed in the NSC  
4 specimens, as illustrated in Fig. 2(a), suggesting gradual concrete crushing took place in these  
5 specimens. On the other hand, in the HSC specimens the damage was highly localized around a  
6 major shear crack, as shown in Fig. 2(b).

### 8 **Axial stress-strain behavior**

9 The summary of the key experimental results are shown in Table 3, which include: the FRP hoop  
10 rupture strains ( $\varepsilon_{h,rupt.}$ ), ultimate axial strength and strain of confined concrete ( $f'_{cc}$  and  $\varepsilon_{cu}$ ), and  
11 strength and strain enhancement ratios ( $f'_{cc}/f'_{co}$  and  $\varepsilon_{cu}/\varepsilon_{co}$ ). The ultimate confined-concrete  
12 strengths  $f'_{cc}$  were calculated from the recorded axial loads just prior to the failure of the  
13 specimens. The ultimate axial strain of confined concrete  $\varepsilon_{cu}$  was averaged from the four LVDTs,  
14 and the hoop rupture strains  $\varepsilon_{h,rupt}$  were averaged from three strain gauge readings, unless stated  
15 otherwise in Table 3. The key specimen performance indicators, namely the strength enhancement  
16 coefficient  $k_1$ , strain enhancement coefficient  $k_2$ , and strain reduction factor  $k_\varepsilon$  are also given in  
17 Table 3. These indicators are discussed in detail later in the paper.

18  
19 Axial stress-strain curves of the cyclically tested specimens of the present study are shown in Fig. 3.  
20 In each of the charts shown in Fig. 3, stress-strain curves of two nominally identical monotonically  
21 loaded specimens are also included for comparison. Figure 3 illustrates that the stress-strain curves  
22 of monotonically loaded specimens exhibit an ascending first branch that is followed by an  
23 ascending or an almost flat second branch. As expected, the stress-strain behavior in the second  
24 branch is influenced significantly by the important confinement parameters, including the  
25 unconfined concrete strength and type and amount of confining material. It can be observed in Fig.  
26 3 that most of the HSC specimens experienced a sudden drop in strength starting right at the



1 transition point on the stress-strain curve. This phenomenon, which can be referred to as 'initial  
2 strength softening', can be associated to the brittle nature of the higher strength concretes. During  
3 this stage, the hoop strains recorded on the FRP jacket increased rapidly and at one point confining  
4 pressures generated by the FRP jacket reached to a level that was high enough to sufficiently  
5 confine the HSC. This point corresponds to the plateau formation on the stress-strain curves shown  
6 in Fig.3, which follows the initial strength softening region. Further increase in the axial strains  
7 leads to either an almost flat or a slightly ascending type of final portion in the stress-strain curve of  
8 FRP-confined HSC specimens as illustrated in Fig. 3. The stress-strain curves of NSC specimens,  
9 on the other hand, are of a continuously ascending type with no signs of softening throughout the  
10 response history, as can be seen in Fig. 3.

11

12 Table 3 shows that the majority of the cyclically loaded specimens exhibit higher compressive  
13 strengths and ultimate axial strains than their monotonically loaded counterparts. A similar  
14 phenomenon was previously reported by other researchers for FRP-confined NSC (Rousakis 2001;  
15 Lam et al. 2006), who demonstrated that load cycles resulted in increased hoop rupture strains  
16 leading to increased compressive strength and ultimate axial strain. These effects are discussed  
17 further in the following sections of the paper. The comparison of the behaviors of otherwise  
18 identical tube encased and wrapped specimens (i.e., H-C-4L-M and H-C-6L-M series specimens) in  
19 Fig. 3 reveals no significant difference between the axial stress-strain behaviors of these specimens.  
20 Therefore, no further consideration is given to the differences of these specimens in the following  
21 discussions.

## 22 **DISCUSSIONS**

### 23 **The envelope curve**

24 The envelope curve of concrete represents the upper boundary of the response of the concrete under  
25 cyclic axial compression. According to the hypothesis proposed by Karsan and Jirsa (1969), a  
26 unique envelope curve exists for a given cyclically loaded concrete specimen and it is identical to

1 the stress-strain curve of the same concrete under monotonic loading. This hypothesis was then  
2 verified by subsequent studies on unconfined and steel-confined concrete, and was shown by Lam  
3 et al. (2006) and Abbasnia and Ziaadiny (2010) to be also valid for FRP-confined concrete.

4  
5 To allow comparisons of the stress-strain curves of monotonically and cyclically tested specimens,  
6 Fig. 3 also shows the envelope curves, which were drawn by connecting the initial unloading points  
7 on the stress-strain curves of cyclically loaded specimens. Figure 3 illustrates that the envelope  
8 stress-strain curves of cyclically loaded specimens closely follow the stress-strain curves of the  
9 corresponding monotonically loaded specimens. This observation is consistent with that reported in  
10 Lam et al. (2006), and supports their conclusion that the basic hypothesis of envelope curves is  
11 valid for FRP-confined concrete.

12

### 13 **Unloading and reloading paths and the plastic strain**

14 To define the complete axial stress-strain response of a cyclically loaded specimen, in addition to  
15 the envelope curve, unloading and reloading paths are also required. An unloading path is defined  
16 as the stress-strain path traced by the concrete as its axial strain reduces, and a reloading path is  
17 defined as the stress-strain path traced by concrete as its axial strain increases from a starting point  
18 on an unloading path (Lam and Teng 2009). Unloading may be from a point on the envelope curve  
19 or from a point on a reloading curve (i.e., before reaching the envelope curve on the reloading path).  
20 All of the cyclically tested specimens of the present study were unloaded from their envelope  
21 curves; thus, herein the term 'unloading' refers to 'envelope curve unloading'. The axial strain at the  
22 starting point of unloading path is referred to as the envelope unloading strain  $\varepsilon_{un,env}$ .

23

24 An unloading path intersects the axial strain axis at a strain value that is referred to as the residual  
25 plastic strain  $\varepsilon_{pl}$ . The residual plastic strain of concrete can be defined as the residual axial strain of  
26 the material when it is unloaded to the zero stress (Lam et al. 2006). Accurate determination of the

1 plastic strains is of vital importance for the overall performance of cyclic axial stress-strain models.  
2 The relationship between  $\varepsilon_{un,env}$  and  $\varepsilon_{pl}$  forms an important aspect of cyclic behavior and has been  
3 investigated in a number of studies for unconfined, steel-confined and FRP-confined concrete (e.g.,  
4 Bahn and Hsu 1998; Sakai, J. and Kawashima 2006; Lam et al 2006; Abbasnia and Ziaadiny 2010).  
5 Lam et al. (2006) demonstrated that the relationship between unloading strains  $\varepsilon_{un,env}$  and plastic  
6 strains  $\varepsilon_{pl}$  was linear for CFRP-confined NSC cylinders for  $\varepsilon_{un,env} \geq 0.0035$ . This observation was  
7 then supported by that of Abbasnia and Ziaadiny (2010), which was based on an experimental  
8 investigation on CFRP-confined NSC square prisms.

9  
10 The relationships between the envelope unloading strains  $\varepsilon_{un,env}$  and estimated plastic strains  $\varepsilon_{pl}$  are  
11 shown in Fig. 4 separately for AFRP-confined NSC, AFRP-confined HSC and CFRP-confined  
12 HSC specimens of the present study. As discussed previously, unloading curves of all the  
13 specimens were terminated just before reaching to zero stress, so the plastic strains were estimated  
14 by extending the unloading curves to cross the axial strain axis. It should also be noted that the  
15 trend lines shown in Fig. 4 are given for the unloading strains that are greater than or equal to  
16 0.0035.

17  
18 A number of important observations can be made from the examination of the trend lines shown in  
19 Figure 4. Firstly, as illustrated in each of the charts shown in Fig. 4, the trend lines of the specimens  
20 of the same concrete strength and confinement material almost coincide, which suggests that the  
21 amount of confinement has little or no influence on the residual plastic strain of FRP-confined  
22 concrete. This observation is in agreement with that previously reported by Lam et al. (2006) on  
23 CFRP-confined NSC, and it suggests that Lam et al.'s original observation is equally applicable to  
24 FRP-confined HSC and concretes confined with different types of FRP (i.e. AFRP and CFRP).  
25 Another important observation is that the comparison of the trend lines of AFRP-confined and  
26 CFRP-confined HSC specimens in Figs. 4(b) and 4(c) indicate that the trend line equation is

1 influenced only slightly by the type of FRP material. Finally, the comparison of the trend line  
 2 equations of NSC and HSC specimens in Fig. 4 indicate that the trend line equation does not change  
 3 significantly with the unconfined concrete strength. This important observation is not in agreement  
 4 with the expression given in Lam and Teng's model (2009) (Eq.1), which predicts a reduction in  
 5 plastic strain  $\varepsilon_{pl}$  with increasing unconfined concrete strength. Eq.1 was calibrated for HSC  
 6 primarily on the extremely limited experimental data reported by Rousakis (2001) on CFRP-  
 7 confined HSC. As illustrated in Fig.5, which shows the comparison of the experimental plastic  
 8 strains with the predictions by Eq.1, the plastic strains of the HSC specimens of the present study  
 9 are largely underestimated by Lam and Teng's model. This is discussed further under 'Comparison  
 10 with existing stress-strain models'.

$$11 \quad \varepsilon_{pl} = (0.87 - 0.004f'_{co})\varepsilon_{un,env} - 0.0016 \quad \text{for} \quad \varepsilon_{un,env} \geq 0.0035 \quad (1)$$

12 To summarize, according to the trend line expressions given in Fig. 4, none of the three important  
 13 specimen parameters investigated in the present study (i.e., the concrete strength, type of FRP, and  
 14 amount of confinement) appear to have significant influence on the relationship between the  
 15 unloading strain  $\varepsilon_{un,env}$  and residual plastic strain  $\varepsilon_{pl}$  of FRP-confined concrete. Another important  
 16 specimen parameter, the shape of the specimen cross-section, has recently been reported by  
 17 Abbasnia and Ziaadiny (2010) to also have only minor influence on the plastic strains of FRP-  
 18 confined concrete. This conclusion was based on the comparison of the trend line equation  
 19 Abbasnia and Ziaadiny (2010) obtained from their CFRP-confined NSC prismatic specimen tests  
 20 with the ones reported by Lam et al. (2006) based on CFRP-confined NSC cylinder tests. It is worth  
 21 noting that the relationships observed between the unloading strains  $\varepsilon_{un,env}$  and plastic strains  $\varepsilon_{pl}$  in  
 22 the present study are in fairly close agreement with those observed in the two aforementioned  
 23 experimental studies, namely Lam et al. (2006) (Eq.2) and Abbasnia and Ziaadiny (2010) (Eq.3).

$$24 \quad \varepsilon_{pl} = \begin{cases} 0.703\varepsilon_{un,env} - 0.0014 & (\text{Series I} - 1\text{-ply CFRP}) \\ 0.716\varepsilon_{un,env} - 0.0016 & (\text{Series II} - 2\text{-ply CFRP}) \end{cases} \quad \text{for} \quad \varepsilon_{un,env} \geq 0.0035 \quad (2)$$

$$\varepsilon_{pl} = 0.747\varepsilon_{un,env} - 0.001 \quad \text{for} \quad \varepsilon_{un,env} > 0.0035 \quad (3)$$

In the existing literature, in addition to the studies cited above, the model proposed by Shao et al. (2006) also provides a set of equations for the calculation of the plastic strains. However, in this model the relationship between the unloading strains and residual plastic strains is not specified explicitly, and plastic strains  $\varepsilon_{pl}$  are calculated by Eq.4 through the use of secant slopes of the unloading curves, which was defined by the originators of the model as the secant modulus of the unloading branch ( $E_{secu}$ ) (Eq.5).

$$\varepsilon_{pl} = \varepsilon_{un,env} - \frac{\sigma_{un,env}}{E_{secu}} \quad (4)$$

$$\frac{E_{secu}}{E_c} = \begin{cases} 1, & 0 \leq \sigma_{un,env} / f'_{co} < 1 \\ -0.44\sigma_{un,env} / f'_{co} + 1.44, & 1 \leq \sigma_{un,env} / f'_{co} < 2.5 \\ 0.34, & \sigma_{un,env} / f'_{co} \geq 2.5 \end{cases} \quad (5)$$

where  $\sigma_{un,env}$  is the stress at the envelope unloading strain, and the elastic modulus of unconfined concrete was defined as  $E_c = 3950\sqrt{f'_{co}}$  (MPa), as originally proposed by Samaan et al. (1998).

The comparison of the experimental plastic strains obtained in the present study with the predictions by Eqs. 4 and 5 from model of Shao et al. (2006) is shown in Fig. 6. The figure illustrates that the plastic strain of the specimens of the present study is overestimated by Shao's model. This shortcoming of the model was originally reported by Lam et al. (2006), and it is caused by the overestimation of the unloading modulus  $E_{secu}$  by Eq.5. At any stage of the loading history beyond the initial elastic portion, with increasing deformations the unloading stiffnesses of both the NSC and HSC specimens of the present study softened much more significantly than that predicted by Eq.5. Furthermore, in Eq.5,  $E_{secu}$  is defined as a function of  $\sigma_{un,env} / f'_{co}$  ratio, according to which  $E_{secu}$  decreases with an increase in  $\sigma_{un,env} / f'_{co}$  ratio. This implies that, for a given unloading strain  $\varepsilon_{un,env}$ , unloading modulus of more heavily confined specimens with steep ascending second

1 branches would be lower than those of their more lightly counterparts. This is not supported by the  
2 observations from the comparison of the unloading curves of neither the NSC (i.e., N-A-2L and N-  
3 A-3L series) nor the HSC (i.e., H-A-4L and H-A-6L) specimens of the present study. In fact, the  
4 results indicate that, for a given  $\varepsilon_{un,env}$  or  $\sigma_{un,env}$ , the unloading stiffnesses of the well-confined  
5 specimens were consistently higher than those of their more lightly confined counterparts. On the  
6 other hand, the final unloading stiffnesses of the NSC specimens of the present study agree well  
7 with the multiplier 0.34 recommended in Eq.5, which suggests an approximately two-thirds  
8 reduction in the initial elastic modulus ( $E_c$ ). However, the slopes of the final unloading curves of  
9 the HSC specimens were significantly steeper, with an  $E_{secu}/E_c$  ratio of approximately 0.65 for the  
10 final unloading cycle, suggesting a much lower degree of stiffness softening. Within the  
11 confinement range considered in the present study,  $E_{secu}/E_c$  ratio is not influenced significantly by  
12 the amount of confinement for neither the HSC nor the NSC specimens. Furthermore, the  
13 comparison of the AFRP- and CFRP-confined HSC specimens indicates that the type of FRP also  
14 has a negligible influence on the final unloading stiffness.

15  
16 Although, as discussed above, Shao's model consistently overestimated the plastic strains of the  
17 specimens of the present, a closer inspection of Fig. 6(a) reveals that for the NSC specimens  
18 confined with 3 layers of AFRP, model predictions of the plastic strains start to become more  
19 accurate at larger axial strain levels. For example, in the last few load cycles of both N-A-3L series  
20 specimens, Shao's model closely predicts the experimental plastic strains. This is due to the way the  
21 unloading modulus  $E_{secu}$  is defined in Eq.5 as a function of  $\sigma_{un,env} / f'_{co}$  ratio. That is, Shao's model  
22 suggests a reduction in the unloading modulus with an increase in the  $\sigma_{un,env} / f'_{co}$  ratio, which in  
23 turn reduces the plastic strain calculated by Eq.3 thereby making them more consistent with  
24 experimentally observed values. Because the strength enhancement due to confinement was not as  
25 pronounced in the other specimens of the present study compared to that experienced by N-A-3L  
26 series specimens, such convergence is not observed in the remaining specimens, as evident in Fig.

1 6. The observations and discussion presented herein suggest that the variation of the stiffness of the  
2 unloading curve can be predicted more accurately through an expression that makes use of  
3 unloading strain to ultimate axial strain ratios ( $\varepsilon_{un,env} / \varepsilon_{cu}$ ) while giving due consideration to the  
4 influence of the unconfined concrete strength on the stiffness softening of the unloading curve. It is  
5 clear that further research on the axial cyclic behavior of FRP-confined concrete is required to  
6 establish these key relationships.

7

### 8 **Ultimate Condition**

9 The ultimate condition of FRP-confined concrete is often characterized as the ultimate strength and  
10 axial strain of concrete recorded at the rupture of the FRP jacket. This, together with the fact that  
11 FRP-confined concrete often exhibits an ascending type of second branch, makes the relationship  
12 between the ultimate strength  $f'_{cc}$ , ultimate axial strain  $\varepsilon_{cu}$  and hoop rupture strain  $\varepsilon_{h,rupt}$  an intimate  
13 one. To better understand this relationship, FRP hoop rupture strains recorded on each test specimen  
14 are reported in Table 3 together with  $f'_{cc}$  and  $\varepsilon_{cu}$ .

15

16 The influence of the key test parameters on the ultimate condition of FRP-confined concrete that  
17 were identified in the preceding section are discussed herein. In order to make a rational assessment  
18 of the influences of unconfined concrete strength and type of FRP, the comparisons were made  
19 between the specimens having similar levels of confinement. Nominal ultimate confinement ratios  
20  $f_{lu}/f'_{co}$ , which are reported in Table 3 and calculated from Eq.6 assuming a uniform confinement  
21 distribution, were used to establish relative confinement levels of the specimens.

22

$$23 \frac{f_{lu}}{f'_{co}} = \frac{2E_f t_f \varepsilon_{fu}}{Df'_{co}} \quad (6)$$

24 where  $E_f$  is the modulus of elasticity,  $t_f$  is the total nominal thickness and  $\varepsilon_{fu}$  is the ultimate tensile  
25 strain of the fibers and  $D$  is the diameter of the specimen.

26

1 It is now well understood, however, that  $f_{lu} / f'_{co}$  ratio calculated from Eq.6 is of theoretical value  
 2 and it does not accurately represent the actual confining pressures developed in the FRP jacket at  
 3 ultimate. As was discussed in a number of studies previously (e.g., Pessiki et al. 2001; Lam and  
 4 Teng 2004; Ozbakkaloglu and Oehlers 2008), this is due to the fact that the ultimate hoop strain  
 5  $\varepsilon_{h,rupt}$  reached in the FRP jacket is often smaller than the ultimate tensile strain of the fibers  $\varepsilon_{fu}$ ,  
 6 which necessitates the use of a strain reduction factor  $k_\varepsilon$  in the calculation of the actual confining  
 7 pressures at ultimate  $f_{lu,a}$

$$8 \quad k_\varepsilon = \frac{\varepsilon_{h,rupt}}{\varepsilon_{fu}} \quad (7)$$

$$9 \quad f_{lu,a} = \frac{2E_f t_f \varepsilon_{h,rupt}}{D} \quad (8)$$

10 Table 3 gives the average strain reduction factors  $k_\varepsilon$  for the specimens of the present study in six  
 11 sub-groups, which were formed based on the concrete strength and FRP type of the specimens, and  
 12 the loading patterns used in testing them. It should be noted that the most damaged sections of the  
 13 specimens not always corresponded to the sections that were instrumented for the measurement of  
 14 the FRP hoop strains. This, at least partly, explains the lower than expected  $k_\varepsilon$  values observed in  
 15 this study. Thus, the strain reduction factors reported in Table 3 are best be treated as lower-bound  
 16 values to be expected from specimens having similar properties to those reported in this study. The  
 17 actual ultimate confinement ratios  $f_{lu,a}/f'_{co}$  that were calculated using the experimentally recorded  
 18 hoop rupture strains  $\varepsilon_{h,rupt}$  are also provided in Table 3 and are used in the calculation of the strength  
 19 and strain enhancement coefficients  $k_1$  and  $k_2$  as discussed in the following section.

20

### 21 ***Effect of Loading Pattern***

22 In Table 3, the comparison of the ultimate strengths and strains of companion specimens that were  
 23 tested either monotonically or cyclically indicates that, in general, both  $f'_{cc}$  and  $\varepsilon_{cu}$  increase with the  
 24 presence of load cycles. Although this observation is true for both NSC and HSC specimens  
 25 confined with AFRP or CFRP, results reported in Table 3 indicate that the observed improvement is



1 more pronounced in AFRP-confined specimens and is particularly notable for N-A-3L and H-A-4L  
2 series specimens. Similar improvements were reported previously by two of the few existing studies  
3 (i.e., Lam et al. (2006) and Demir et al. (2010)) that looked into the influence of unloading and  
4 reloading cycles on the ultimate condition of FRP-confined concrete. On the other hand, the average  
5  $k_\varepsilon$  values reported in Table 3 suggest that load cycles did not have a pronounced effect on the  
6 recorded hoop rupture strains. This observation does not agree well with the one reported herein  
7 regarding the influence of load cycles on the ultimate strength and axial strain of FRP-confined  
8 concrete. Furthermore, both Lam et al. (2006) and Demir et al. (2010) reported an observed increase  
9 in the hoop rupture strains in the presence of unloading/reloading cycles. It is clear that further  
10 research is required on the axial cyclic behavior of FRP-confined concrete to better understand the  
11 influence of load cycles on the development of FRP hoop strains and on the strain reduction factor  
12  $k_\varepsilon$ .

13

#### 14 ***Effect of Unconfined Concrete Strength***

15 Comparison of N-A-2L and H-A-6L series specimens in Table 3, which had similar  $f_{lu} / f'_{co}$  ratios,  
16 indicate that both the ultimate strength and strain enhancement ratios ( $f'_{cc} / f'_{co}$  and  $\varepsilon_{cu} / \varepsilon_{co}$ ) are  
17 lower for HSC specimens than for NSC specimens under both monotonic and cyclic loading  
18 conditions. Another important observation from Table 3 is that  $k_\varepsilon$  values of HSC specimens are  
19 consistently lower than those of NSC specimens. This observation, which is also supported by those  
20 from the other recent studies conducted by the first Author's research group at the University of  
21 Adelaide (Wang 2009; Li 2011), suggests that strain reduction factor  $k_\varepsilon$  is concrete strength  
22 dependant. Furthermore, although it was not directly stated by the authors of the original studies, a  
23 similar trend can be observed from the test results of a few other studies reported in the literature on  
24 FRP-confined HSC (Eid et al. 2009; Cui and Sheikh 2010; Xiao 2010). Further research on FRP-  
25 confined HSC is required for an in-depth examination of this important observation.

26

1 Lower recorded hoop rupture strains can, at least partly, explain the lower strength and strain  
 2 enhancement ratios ( $f'_{cc} / f'_{co}$  and  $\varepsilon_{cu} / \varepsilon_{co}$ ) observed in the HSC specimens of the present study.  
 3 However, to demonstrate that the performance difference between the NSC and HSC specimens  
 4 cannot be explained exclusively by the lower hoop rupture strains of the HSC specimens, strength  
 5 and strain enhancement coefficients ( $k_1$  and  $k_2$ ) were calculated and are presented in Table 3 for  
 6 each series of specimens. These values were based on the general form of one of the most widely  
 7 recognized ultimate condition expressions reported in the literature by Lam and Teng (2003):

$$8 \quad \frac{f'_{cc}}{f'_{co}} = 1 + 3.3 \frac{f_{lu,a}}{f'_{co}} \quad (9)$$

$$10 \quad \frac{\varepsilon_{cu}}{\varepsilon_{co}} = 1.75 + 12 \left( \frac{f_{lu,a}}{f'_{co}} \right) \left( \frac{\varepsilon_{h,rupt}}{\varepsilon_{co}} \right)^{0.45} \quad (10)$$

11 Strength and strain enhancement coefficients ( $k_1$  and  $k_2$ ) given in Table 3 were calculated from the  
 12 experimental results by replacing the constant values given in Eqs. 9 and 10 of Lam and Teng's  
 13 model (i.e., 3.3 and 12) with  $k_1$  and  $k_2$ , respectively. It can be seen in Table 3 that the average  
 14 values of both the strength and strain enhancement coefficients are consistently lower for the HSC  
 15 specimens than the NSC specimens even when reduced  $k_\varepsilon$  values are applied in calculating the  
 16 actual confining pressures  $f_{lu,a}$  of the HSC specimens. This suggests that direct application of the  
 17 existing ultimate condition expressions, which were based almost exclusively on test data from  
 18 FRP-confined NSC, to FRP-confined HSC can lead to significant overestimations of the ultimate  
 19 conditions. In particular, the strength enhancement of FRP-confined HSC would be largely  
 20 overestimated by these expressions if they are to be applied to lightly or moderately confined HSC,  
 21 such as H-C-4L, H-C-6L and H-A-4L series specimens of the present study. As has also recently  
 22 been stated by Xiao et al (2010), it is clear that much more work is needed to better understand the  
 23 behavior of FRP-confined HSC.  
 24  
 25  
 26

27 ***Effect of FRP Type***

1 Comparison of H-A-4L and H-C-6L series specimens in Table 3, which had similar concrete  
2 strengths and confining pressures, indicates a similar level of strength enhancement ( $f'_{cc}/f'_{co}$ ) for  
3 the AFRP- and CFRP-confined specimens. On the other hand, the level of strain enhancement ( $\varepsilon_{cu}$   
4  $/\varepsilon_{co}$ ) observed in the AFRP-confined specimens is significantly higher than that in the CFRP-  
5 confined specimens. This was expected, as the dependency of the ultimate strain enhancement ratio  
6 to the rupture strain of the confinement material, or rather to the hoop rupture strain, has been  
7 documented previously (e.g. Lam and Teng 2003, 2004) and has now been incorporated into some  
8 of the more accurate FRP confinement models.

9  
10 The comparison of the average  $k_\varepsilon$  values given in Table 3 for the AFRP- and CFRP-confined HSC  
11 specimens, suggests that the type of FRP does not have significant influence on  $k_\varepsilon$ . This  
12 observation, however, is not in agreement with the findings of an on-going research by the first  
13 author's research group at the University of Adelaide on the behavior of FRP-confined HSC (Li  
14 2011), where higher  $k_\varepsilon$  values have been observed for AFRP-confined concrete compared to CFRP-  
15 confined concrete. Similar observations about the higher  $k_\varepsilon$  values of AFRP-confined concrete over  
16 CFRP-confined concrete have recently been reported by Dai et al. (2011) based on their  
17 experimental studies on FRP-confined NSC. Interestingly, however, despite the favorable behavior  
18 of the AFRP-confined concrete as demonstrated by the results of the present study, the area remains  
19 largely under-investigated, with majority of the existing studies on FRP-confined concrete focusing  
20 on the use of CFRP and GFRP as concrete confinement. Thus, further research is required to better  
21 understand how the strain reduction factor  $k_\varepsilon$  is influenced by the type of FRP.

### 22 23 ***Effect of Amount of Confinement***

24 It is well understood that there is an intimate relationship between the amount of confinement and  
25 the ultimate condition of FRP-confined concrete, and that both the strength and strain enhancement  
26 ratios ( $f'_{cc}/f'_{co}$  and  $\varepsilon_{cu}/\varepsilon_{co}$ ) increase with increasing confinement ratio ( $f_{lu,a}/f'_{co}$ ). However, a closer

1 inspection of the strength enhancement coefficients ( $k_I$ ) reported in Table 3 reveals that, for the  
2 HSC specimens the relationship between  $f'_{cc}/f'_{co}$  and  $f_{lu,a}/f'_{co}$  is not a linear one as suggested by  
3 Eq.9. That is, for each series of HSC specimens,  $k_I$  increases with increasing confinement  
4 thickness. This can be best explained by referring to the trend of the stress-strain relationships of the  
5 HSC specimens shown in Figs. 3(i) and 3(j). For example, the overall descending trend of the  
6 second branch of H-C-4L series specimens suggest that confinement provided by 4 layers of 0.117  
7 mm CFRP was not sufficient to provide strength enhancement in 152.5 mm 103 MPa concrete  
8 cylinders. As can be seen in Figs. 3(k) and 3(l), when the number of CFRP layers were increased to  
9 6, the specimens (H-C-6L series) exhibited a slightly ascending second branch. It is evident from  
10 this comparison that strength enhancement is observed only when the concrete is confined by a  
11 confinement system providing a higher than a minimum amount of confinement, which can be  
12 defined as threshold confinement amount. Therefore, it can be said that only the part of confinement  
13 that is over this threshold value contributes directly to the strength enhancement of FRP-confined  
14 concrete. Recent experimental studies conducted by the first author's research group at the  
15 University of Adelaide indicate that this threshold amount is highly sensitive to the concrete  
16 strength and can be up to 10 times as high for ultra HSC of around 120 MPa strength as for standard  
17 30 MPa NSC (Wang 2009; Li 2011). As a result, calculation of  $k_I$  values using the form of Eq.9  
18 that gives no consideration to the threshold confinement amount, leads to extremely low  $k_I$  values  
19 for lightly confined HSC specimens (such as H-A-4L and H-C-6L series) as shown in Table 3. It is  
20 clear from these observations that for better prediction of the ultimate strength of FRP-confined  
21 HSC, there is need for a new expression that can accurately predict the threshold ratio as a function  
22 of the concrete strength, and another expression that incorporates this ratio for the calculation of the  
23 strength enhancement ratios.

24

25 Results reported in Table 3 further indicate that, apart from the variations of  $k_I$  values for the HSC  
26 specimens discussed above, for a given series of specimens, strength and strain enhancement

1 coefficients  $k_1$  and  $k_2$  do not vary significantly with the amount of confinement, suggesting an  
2 overall agreement with the forms of Eqs. 9 and 10.

3

#### 4 **COMPARISON WITH EXISTING STRESS-STRAIN MODELS**

5 In this section, the results of the present study are compared with the cyclic axial stress-strain  
6 models developed by Shao et al. (2006) and Lam and Teng (2009). The details of these models can  
7 be found in the original papers, and hence are not discussed herein. Figure 7 shows the comparisons  
8 of the experimental stress-strain curves with the predictions of Shao's and Lam and Teng's models  
9 for two NSC specimens N-A-2L-C1 and N-A-3L-C1 and a HSC specimen H-A-6L-C1. In Shao's  
10 model, the stress-strain model for monotonic behavior proposed by Samaan et al. (1998) was used  
11 to predict the envelope curve and the curve shape parameter ( $n$ ) of the model was adjusted to attain  
12 the best fit with the experimental curves. In Lam and Teng's model, the researchers' monotonic  
13 stress-strain model (Lam and Teng 2003) was used for the prediction of the envelope curve. In the  
14 present study, although the shape of the envelope curves was determined based on the expressions  
15 proposed by the originators of the models, the test results reported in Table 3 were used to  
16 determine the ultimate conditions (i.e.  $f'_{cc}$  and  $\epsilon_{cu}$ ), as there were some differences between the  
17 experimental values and model predictions.

18 Figure 7 illustrates that Lam and Teng's model is highly accurate in predicting both the unloading  
19 and reloading paths of FRP-confined NSC. In predicting these paths, both the shapes of the  
20 unloading and reloading curves and the predicted values of plastic strains play an important role. As  
21 evident from both Fig. 5(a) and Figs 7(b) & 7(d), Lam and Teng's model closely predicts the plastic  
22 strains of the NSC specimens of the present study, with only a very slight underestimation. Because  
23 Shao's model over-predicts the plastic strains, as illustrated in Fig. 6 and discussed in the previous  
24 section, model predictions of the unloading and reloading curves deviate from the experimentally  
25 recorded ones in the majority of the load cycles, as shown in Figs. 7(a), 7(c) and 7(e). Furthermore,  
26 as was also previously noted by Lam et al (2006), the shape of the unloading curves predicted by

1 Shao's model does not accurately capture the shape of the experimental curves. On the other hand,  
2 provided that reloading initiates at a correctly determined plastic strain, both models predict the  
3 reloading paths reasonably accurately, with the parabolic portion defined in Lam and Teng's model  
4 for the region where reloading path returns to the envelope curve providing more accurate  
5 representation of the experimental curves compared to the fully linear reloading curve given by  
6 Shao's model. This is evident from the curves of the NSC specimens shown in Figs 7(a) to 7(d).

7  
8 Application of both models to the HSC specimens, however, lead to large errors in the estimations  
9 of the stress-strain curves as illustrated in Figs. 7(e) & 7(f). In the case of Lam and Teng's model,  
10 the deviation from the experimental curves is caused largely by the inaccuracies in the calculation  
11 of the plastic strains. The plastic strains calculated by Eq.1 from Lam and Teng's model are not in  
12 agreement with the experimentally observed values for the HSC specimens of the present study, as  
13 illustrated in Figs. 5(b) & 5(c) and discussed previously. It should be noted that, due to the  
14 extremely limited nature of the data available in the literature on the axial cyclic behavior of FRP-  
15 confined HSC, Eq. 1 in Lam and Teng's model was calibrated for HSC by using only a few  
16 unloading/reloading cycles originally reported by Rousakis (2001) for CFRP-confined HSC. Figure  
17 7(f) illustrates that the performance of Lam and Teng's model degrades greatly when the model is  
18 applied to FRP-confined HSC. However, the features of the model that works well for NSC appears  
19 to also work well for HSC and the unsatisfactory performance appears to be caused largely by  
20 significant underestimation of the experimental plastic strains by Eq. 1. For Lam and Teng's model,  
21 which closely predicts the response of FRP-confined NSC, to provide similar levels of accuracy for  
22 higher strength concretes, Eq. 1 has to be revised using a larger and more reliable test database.  
23 Figure 7(e) illustrates that, unlike Lam and Teng's model, Shao's model's performance does not  
24 degrade when the model is applied to HSC, but neither does it improve; that is, the aforementioned  
25 shortcomings of the model observed for NSC is also present when the model is applied to HSC.  
26 Finally, it is worth noting that it was not possible to accurately predict the envelope curves of the

1 HSC specimens of the present study using one of the many existing design-oriented stress-strain  
2 models developed for FRP-confined monotonic axial compression. This suggests that none of the  
3 existing stress-strain models proposed for FRP-confined concrete is capable of predicting the stress-  
4 strain relationship of FRP-confined HSC accurately.

5

## 6 **CONCLUSIONS**

7 This paper has presented the results of an experimental study on the behavior of FRP-confined NSC  
8 and HSC under axial compression. Results from monotonic and cyclic compression tests on AFRP  
9 and CFRP-confined concrete specimens have been presented and discussed. The test results have  
10 also been compared with two cyclic axial stress-strain models for FRP-confined concrete. Based on  
11 the results and discussions presented in the paper the following conclusions can be drawn:

12

- 13 1. The envelope stress-strain curve of cyclically loaded FRP-confined concrete closely follows the  
14 stress-strain curve of the same concrete under monotonic loading. This is shown to be true for  
15 CFRP-confined HSC and AFRP-confined NSC and HSC.
- 16 2. The residual plastic strain of FRP-confined concrete is linearly related to the envelope  
17 unloading strain, and this relationship does not appear to be influenced significantly by: i) the  
18 amount of confinement; ii) the type of FRP; and iii) the unconfined concrete strength.
- 19 3. In general, the presence of unloading/reloading cycles leads to an increase in the ultimate  
20 strength and strain of FRP-confined concrete.
- 21 4. For a given actual confinement ratio  $f_{lu,d}/f'_{co}$ , both the strength enhancement and strain  
22 enhancement ratios decrease with the increase of unconfined concrete strength. Furthermore, the  
23 average hoop rupture strain  $\varepsilon_{h,rupt}$  also decreases with increasing unconfined concrete strength.  
24 Therefore, direct application of the existing FRP-confined concrete stress-strain models to FRP-  
25 confined HSC can lead to significant overestimation of the ultimate condition of FRP-confined  
26 HSC.

1 5. Concrete experiences a similar level of strength enhancement when confined with AFRP and  
2 CFRP jackets that provide the same actual confining pressure  $f_{lu,a}$ . On the other hand, the  
3 ultimate strain of the same concrete increases more significantly through AFRP confinement.

4 In addition to the general conclusions of the experimental study reported herein, the following  
5 observations can be made based on the comparison of the test results of the present study with two  
6 cyclic axial stress-strain models for FRP-confined concrete:

- 7  
8 • The axial cyclic stress-strain model proposed by Lam and Teng (2009) is highly accurate in  
9 predicting both the unloading and reloading paths of FRP-confined NSC. The model closely  
10 predicts the shapes of the unloading and reloading curves and accurately estimates the plastic  
11 strains. When the model is applied to HSC specimens, on the other hand, the model predictions  
12 deviate significantly from the experimental results; this is caused largely by the inaccuracies in  
13 the calculation of the plastic strains of FRP-confined HSC.
- 14 • Comparisons between the results of the present study and the predictions of the cyclic stress-  
15 strain model proposed by Shao et al. (2006) indicated that this model predicts the reloading  
16 paths reasonably accurately, but it consistently overestimates the residual plastic strains and  
17 does not accurately capture the shape of the unloading paths.

18  
19 Finally, it is important to note that among over 50 design-oriented monotonic stress-strain models  
20 published in the literature none is able to correctly predict the stress-strain behavior of FRP-  
21 confined HSC. There is a need for a stress-strain model that can accurately predict the monotonic  
22 behavior of FRP-confined HSC, and more work is required to better understand and model the  
23 behavior of FRP-confined HSC.

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Table 1. Properties of test specimens

Loading pattern	Confinement Material	Number of FRP Layers	Specimen	$f'_{co}$ (MPa)	$\epsilon_{co}$ (%)		
Monotonic	AFRP	2	N-A-2L-M1	39	0.21		
			N-A-2L-M2	39	0.21		
		3	N-A-3L-M1	39	0.21		
			N-A-3L-M2	39	0.21		
		4	H-A-4L-M1	100	0.34		
			H-A-4L-M2	102	0.34		
		6	H-A-6L-M1	106	0.35		
			H-A-6L-M2	106	0.35		
		CFRP	4	H-C-4L-M1*	100	0.34	
				H-C-4L-M2	108	0.35	
			6	H-C-6L-M1	110	0.35	
				H-C-6L-M2*	94	0.33	
		Cyclic	AFRP	2	N-A-2L-C1	38	0.21
					N-A-2L-C2	39	0.21
3	N-A-3L-C1			39	0.21		
	N-A-3L-C2			39	0.21		
4	H-A-4L-C1			100	0.34		
	H-A-4L-C2			102	0.34		
6	H-A-6L-C1			104	0.34		
	H-A-6L-C2			106	0.35		
CFRP	4			H-C-4L-C1	100	0.34	
				H-C-4L-C2	100	0.34	
	6			H-C-6L-C1	109	0.35	
				H-C-6L-C2	105	0.35	

\*FRP tube-encased

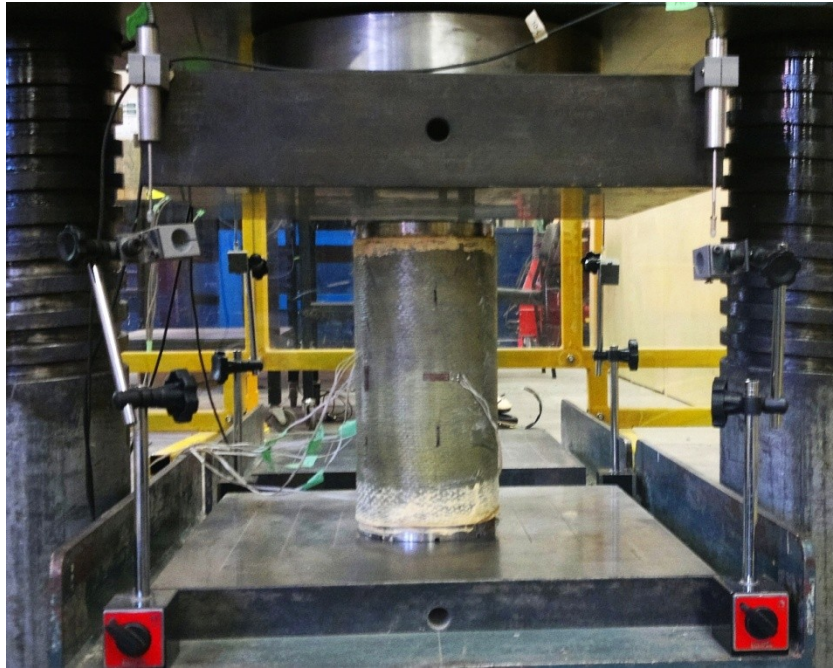
Table 2. Properties of fiber sheets as provided by the manufacturer

Type	Nominal thickness $t_f$ (mm/ply)	Tensile strength $f_{tu}$ (MPa)	Ultimate tensile strain $\varepsilon_{tu}$ (%)	Elastic modulus $E_f$ (GPa)	Weight (g/m <sup>2</sup> )
Carbon	0.117	3800	1.55	240	200
Aramid	0.200	2900	2.50	120	290

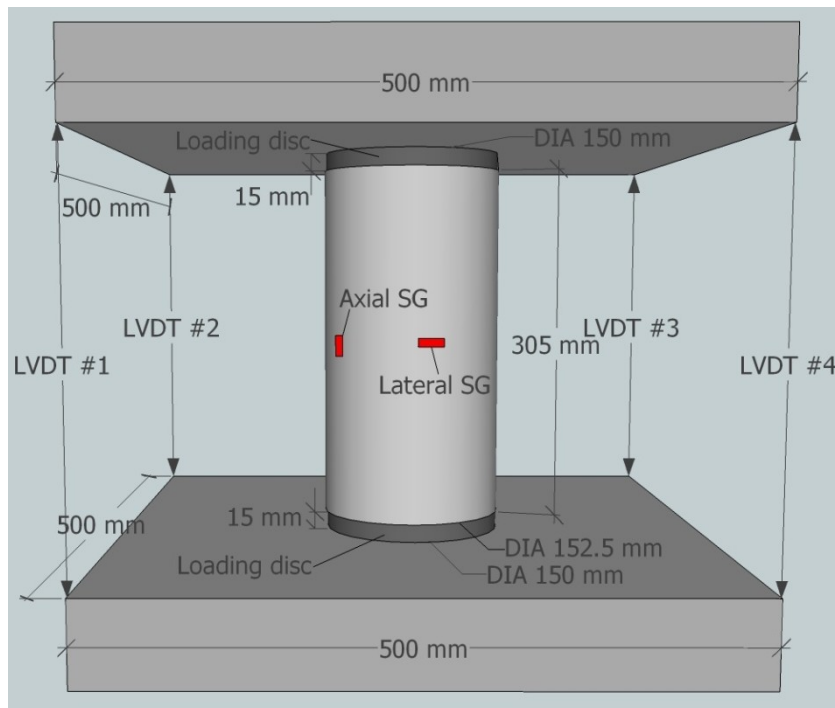
Table 3. Test results of FRP-confined concrete cylinders

Specimen	$f'_{cc}$ (MPa)	$\epsilon_{cu}$ (%)	$\epsilon_{h,rupt}$ (%)	$f_{lu}/f'_{co}$	$f_{lu2}/f'_{co}$	$f'_{cc}/f'_{co}$ Average	$\epsilon_{cu}/\epsilon_{co}$ Average	$k_1$ Average	$k_2$ Average	$k_\epsilon$ Average
N-A-2L-M1	69.2	2.32	1.71	0.40	0.28	1.75	10.9	2.82	13.8	0.68
N-A-2L-M2	67.1	2.30	1.56	0.40	0.25					
N-A-3L-M1	85.0	2.86	1.66	0.61	0.40	2.21	14.1	2.86	11.2	
N-A-3L-M2	87.6	3.11	1.84	0.61	0.45					
H-A-4L-M1	122.3	1.45	1.18*	0.32	0.15	1.19	4.0	1.26	8.4	0.46
H-A-4L-M2	118.7	1.29	1.29	0.31	0.16					
H-A-6L-M1	154.7	1.70	1.10*	0.45	0.20	1.45	4.9	2.33	9.7	
H-A-6L-M2	153.2	1.70	1.07	0.45	0.19					
H-C-4L-M1	98.9	0.93	0.89	0.23	0.13	0.97	2.7	N/A	5.5	0.55
H-C-4L-M2	103.3	0.96	0.81	0.21	0.11					
H-C-6L-M1	122.3	1.13	0.94	0.31	0.19	1.22	3.4	1.17	5.8	
H-C-6L-M2	124.4	1.16	0.78	0.37	0.18					
N-A-2L-C1	64.3	2.25	1.50	0.42	0.25	1.67	10.7	2.67	14.6	0.68
N-A-2L-C2	64.3	2.25	1.56	0.40	0.25					
N-A-3L-C1	97.4	4.04	1.76	0.61	0.43	2.59	20.0	3.46	14.9	
N-A-3L-C2	104.5	4.43	2.02	0.61	0.49					
H-A-4L-C1	136.4	1.82	1.24	0.32	0.16	1.30	5.1	2.00	13.1	0.50
H-A-4L-C2	125.4	1.63	1.10	0.31	0.14					
H-A-6L-C1	157.2	1.87	1.16	0.46	0.21	1.56	5.8	2.39	9.5	
H-A-6L-C2	170.9	2.13	1.45	0.45	0.26					
H-C-4L-C1	102.3	1.07	0.69	0.23	0.10	0.99	3.2	N/A	8.9	0.48
H-C-4L-C2	96.0	1.06	0.81*	0.23	0.12					
H-C-6L-C1	123.7	1.14	0.64	0.31	0.13	1.19	3.3	1.21	7.6	
H-C-6L-C2	129.9	1.16	0.81	0.33	0.17					

\* The average hoop rupture strain was calculated from 2 strain gauges.



(a)



(b)

Figure 1. Test setup used in axial compression tests: (a) Specimen before testing; (b) Technical illustration



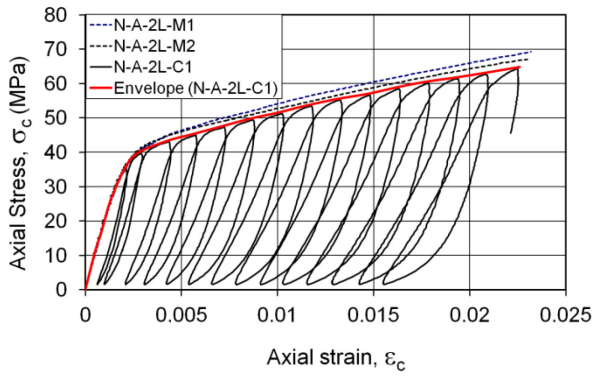


(a)

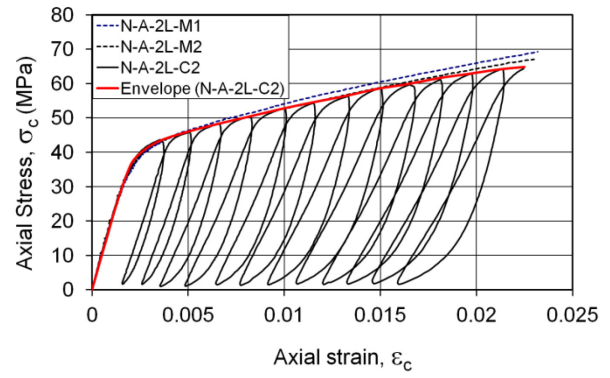


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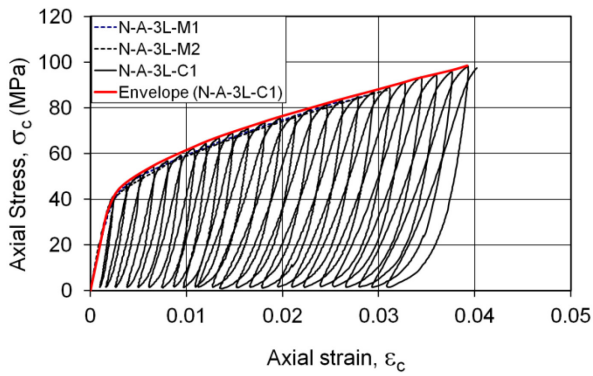
Figure 2. Typical failure modes of test specimens: (a) NSC specimen; (b) HSC specimen



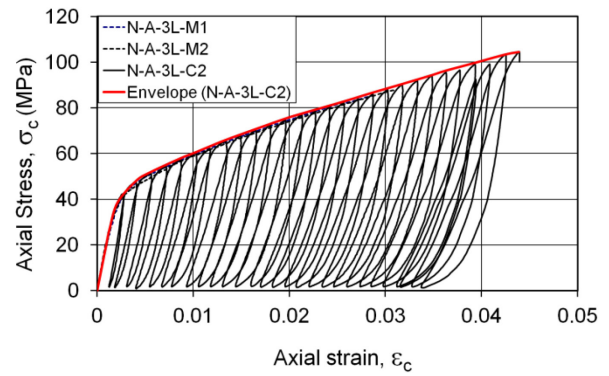
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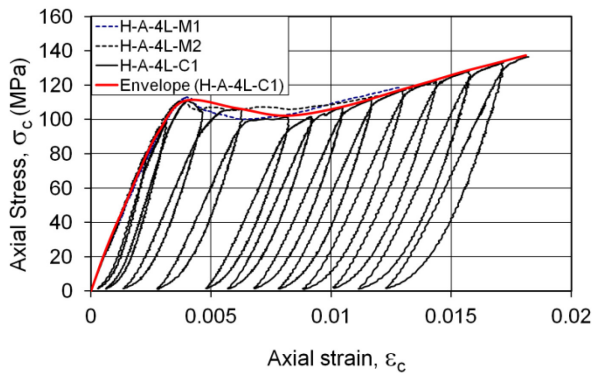
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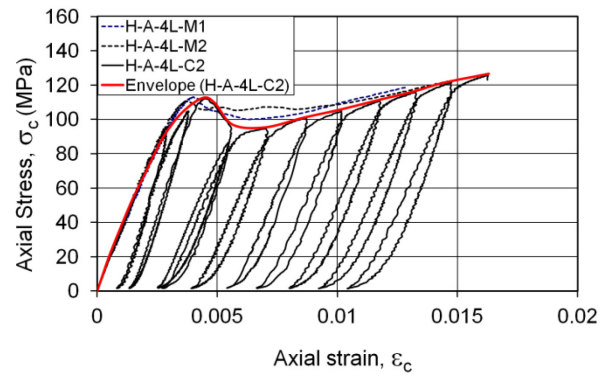
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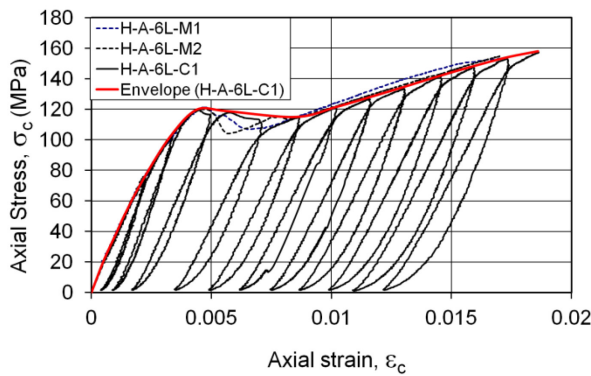
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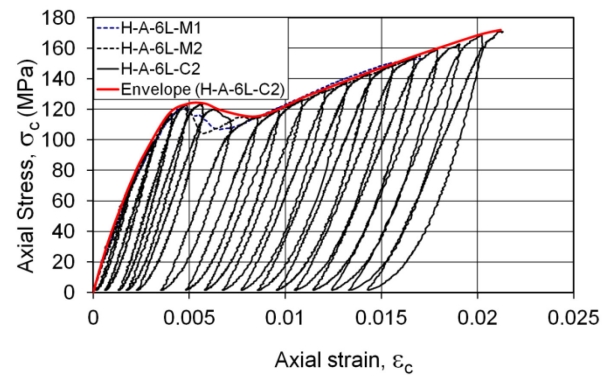
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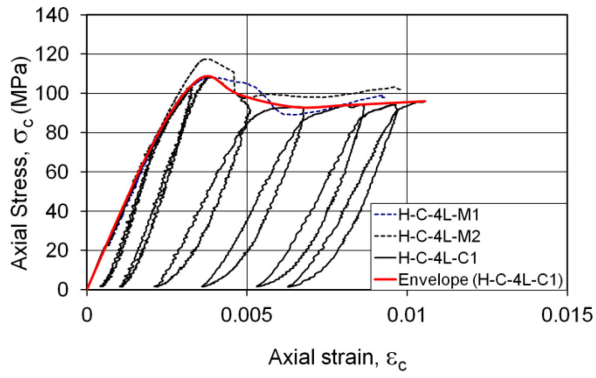
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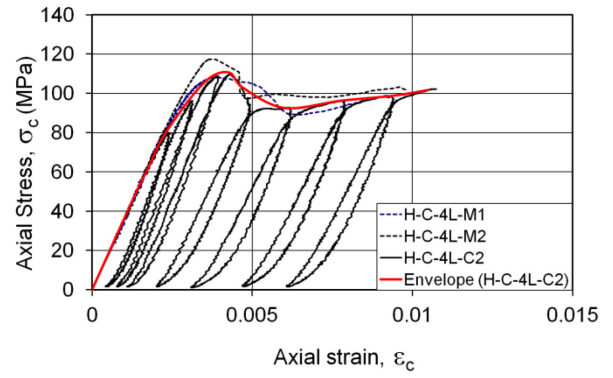
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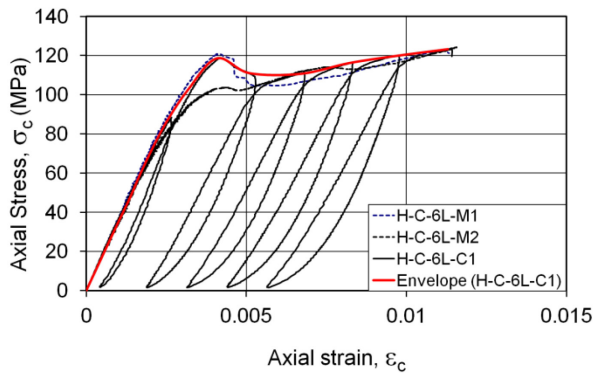
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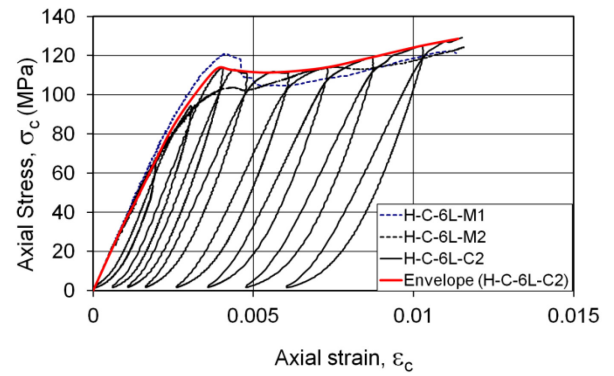
(i)



(j)

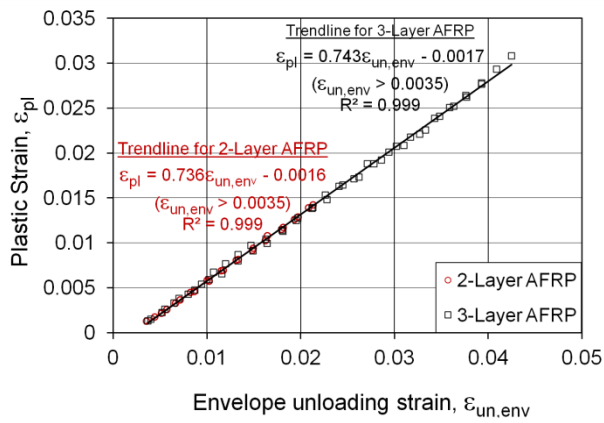


(k)

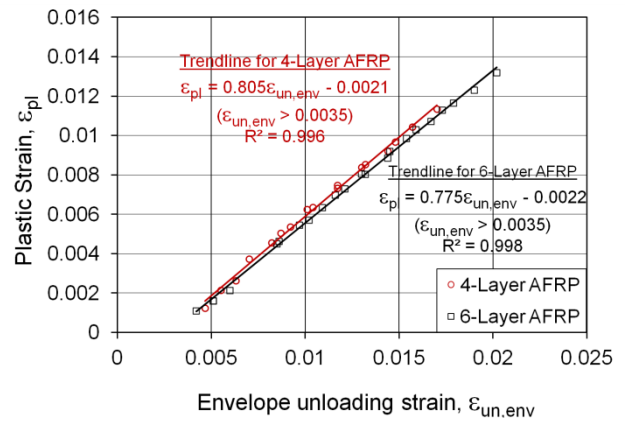


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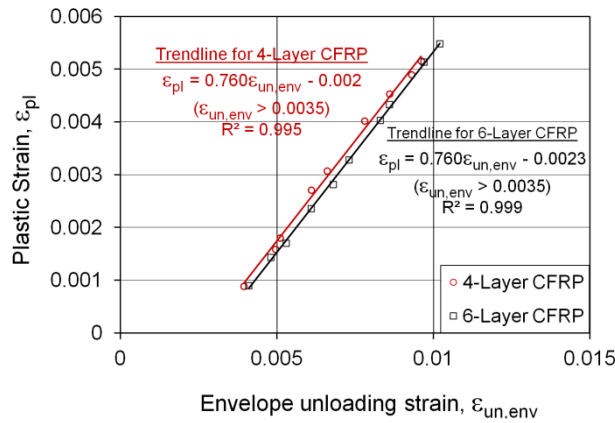
Figure 3. Axial stress-strain curves of test specimens: (a) N-A-2L Series-1; (b) N-A-2L Series-2; (c) N-A-3L Series-1; (d) N-A-3L Series-2; (e) H-A-4L Series-1; (f) H-A-4L Series-2; (g) H-A-6L Series-1; (h) H-A-6L Series-2; (i) H-C-4L Series-1; (j) H-C-4L Series-2; (k) H-C-6L Series-1; (l) H-C-6L Series-2



(a)

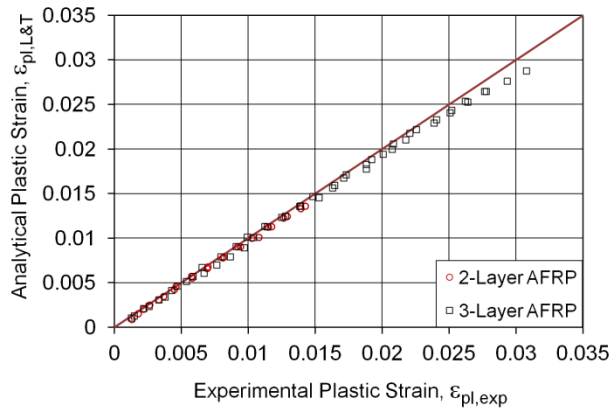


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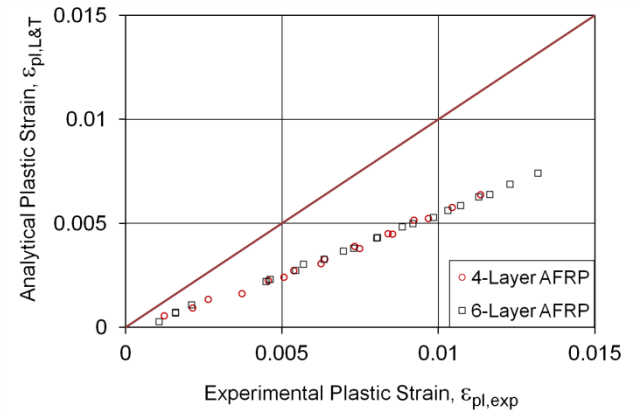


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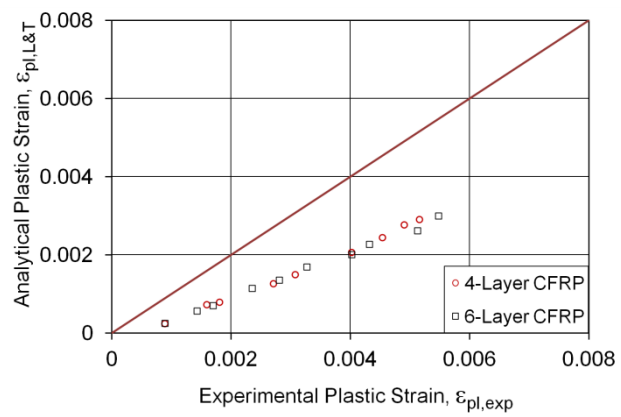
Figure 4. Plastic strain-envelope unloading strain relationships of test specimens: (a) AFRP-confined NSC; (b) AFRP-confined HSC; (c) CFRP-confined HSC



(a)

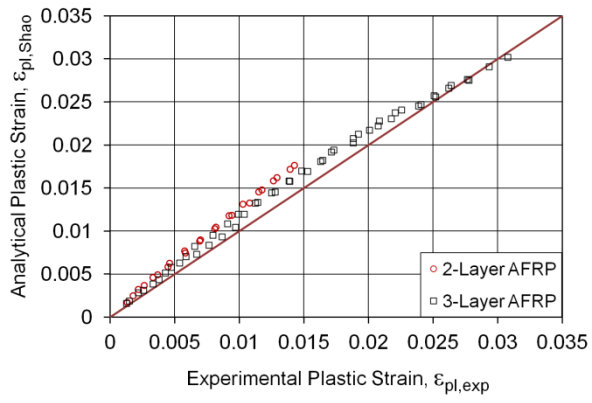


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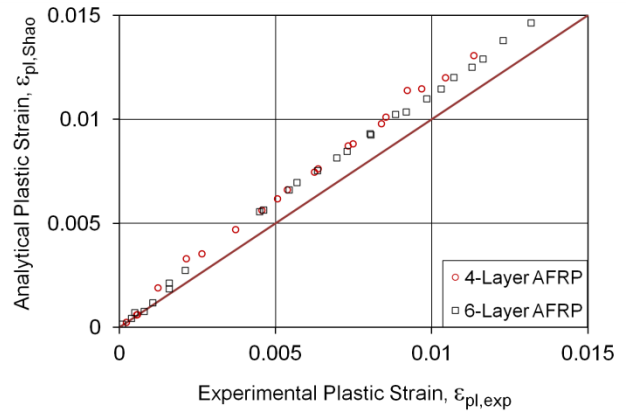


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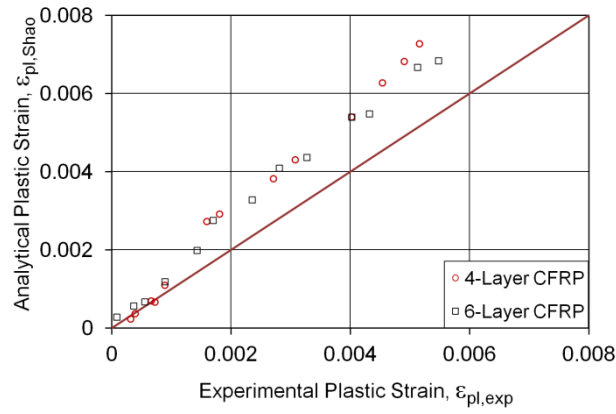
Figure 5. Comparison of experimentally recorded plastic strains with predictions of Lam and Teng's model: (a) AFRP-confined NSC; (b) AFRP-confined HSC; (c) CFRP-confined HSC



(a)



(b)



(c)

Figure 6. Comparison of experimentally recorded plastic strains with predictions of Shao's model: (a) AFRP-confined NSC; (b) AFRP-confined HSC; (c) CFRP-confined HSC

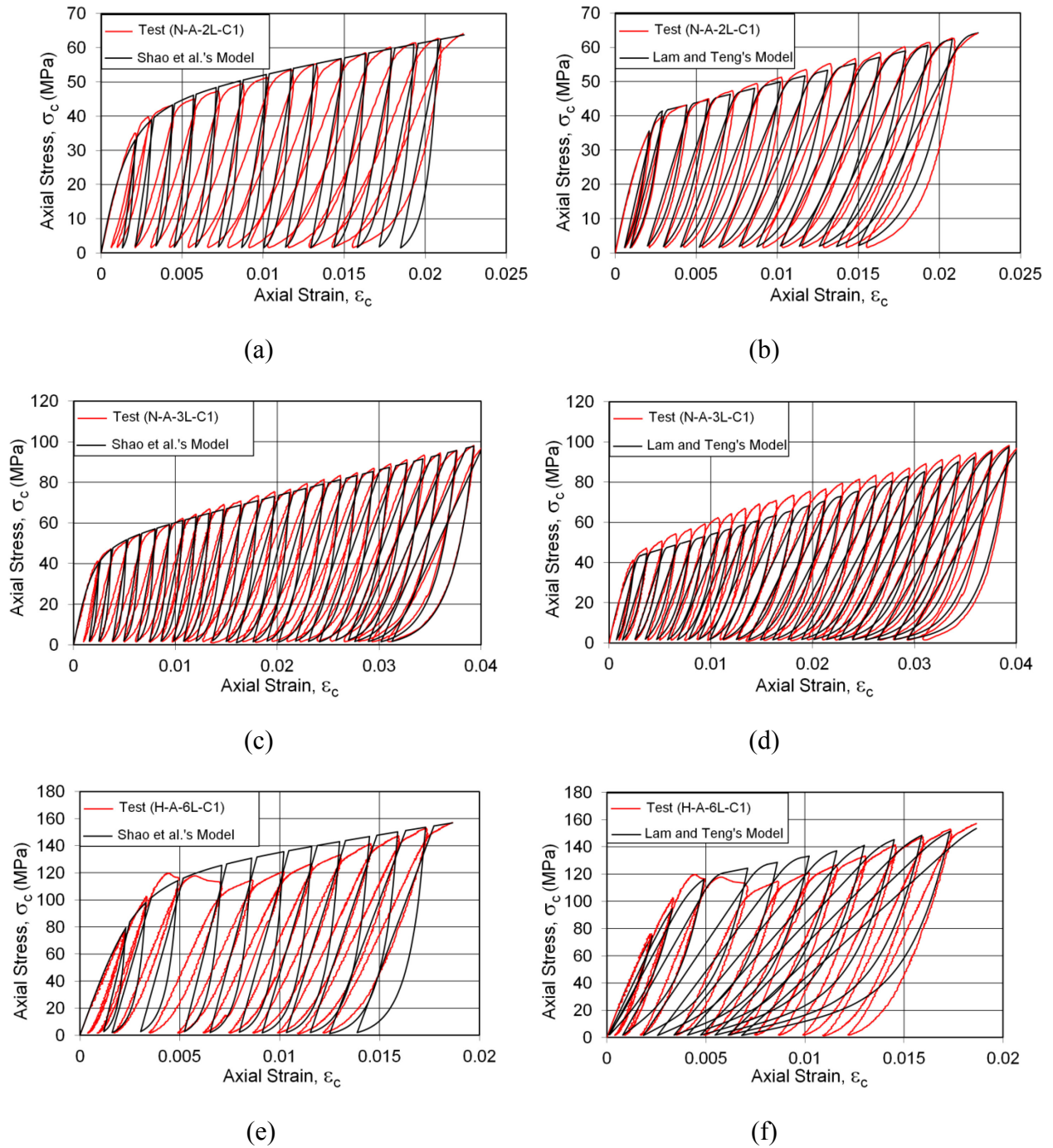


Figure 7. Comparison of experimental cyclic stress-strain curves with predictions of Shao's and Lam & Teng's models: (a) Specimen N-A-2L-C1 vs Shao's model; (b) Specimen N-A-2L-C1 vs Lam & Teng's model; (c) Specimen N-A-3L-C1 vs Shao's model (d) Specimen N-A-3L-C1 vs Lam & Teng's model; (e) Specimen H-A-6L-C1 vs Shao's model (f) Specimen H-A-6L-C1 vs Lam & Teng's model.